

# Coping with Climate Uncertainty in Projected Ranges of Pests Using Hypervolumes



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# Introduction

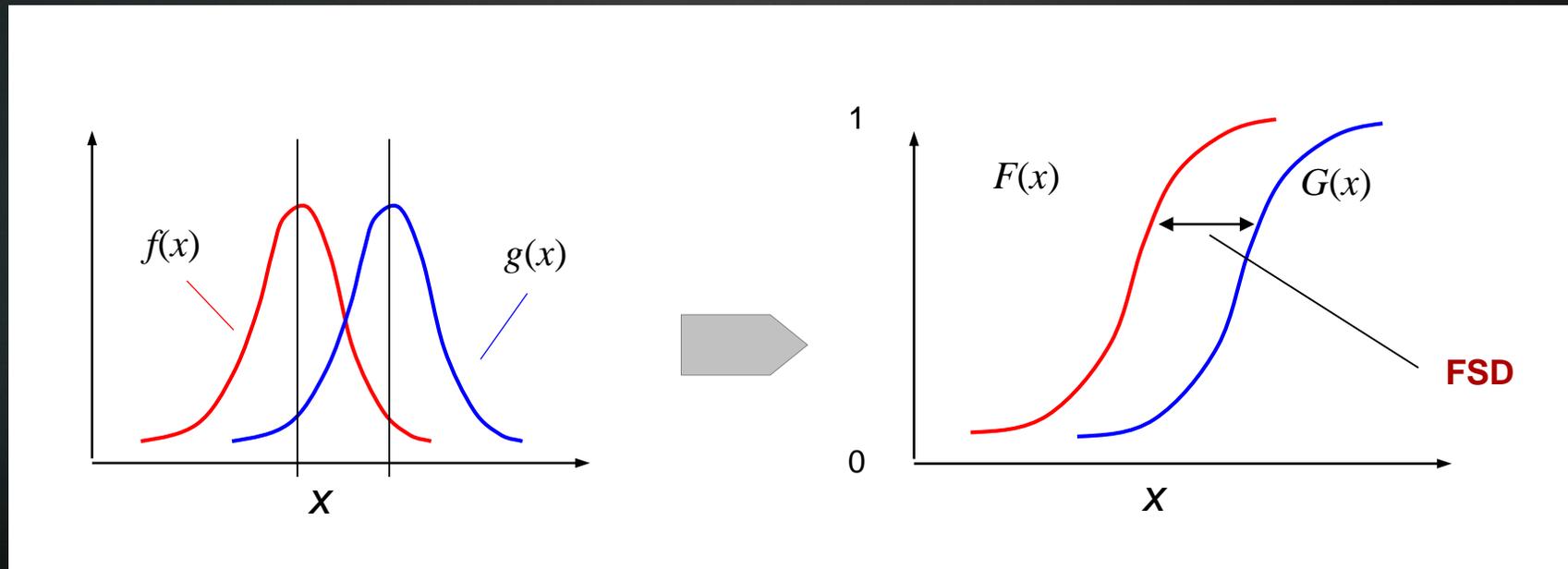
- ▶ Modeling suitable ranges of invasive species under climate change
  - ▶ Many GCMs and emission scenarios, plus time = many plausible outcomes
  - ▶ Thus highly uncertain predictions
  - ▶ Limited uptake by decision makers

# Managing uncertainty in projected suitable ranges

- ▶ How to handle uncertain projections?
- ▶ Averaging ignores uncertainty
- ▶ Other approaches incorporate uncertainty directly
- ▶ For example, methods using stochastic efficiency

# First-degree stochastic dominance (FSD)

- ▶ Comparing two stochastic variables,  $f(x)$  and  $g(x)$
- ▶ Using their cumulative distribution functions,  $F(x)$  and  $G(x)$
- ▶ In this example,  $G(x)$  dominates  $F(x)$



# Non-dominant subsets

- ▶ Can use FSD to find non-dominant subsets of a set
  - ▶ e.g., pixels/locations in a map
  - ▶ Each has a CDF of plausible values
  - ▶ Compare via FSD to place them in subsets
- ▶ These non-dominant subsets can be ordered
- ▶ Thus, FSD = ordinal measure that incorporates uncertainty
- ▶ Hypervolume approach takes this further, arranging the non-dominant subsets in continuous space

# Hypervolumes: a geometric illustration

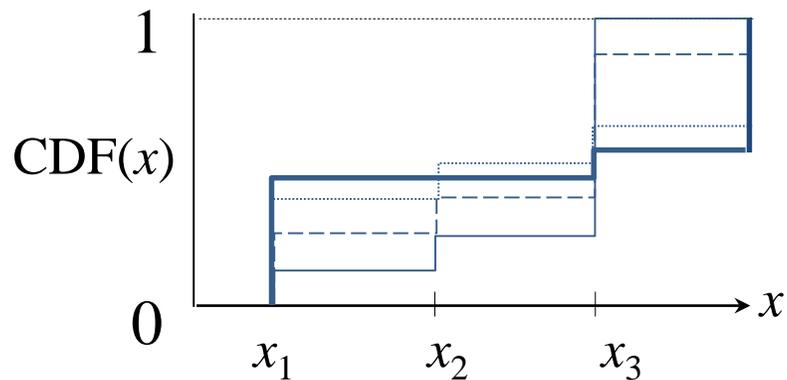
Consider a set  $A$  of four CDFs sampled at discrete points  $x_1, x_2, x_3$ :

CDF 1: (0.25, 0.375, 0.875)

CDF 2: (0.375, 0.5, 0.625)

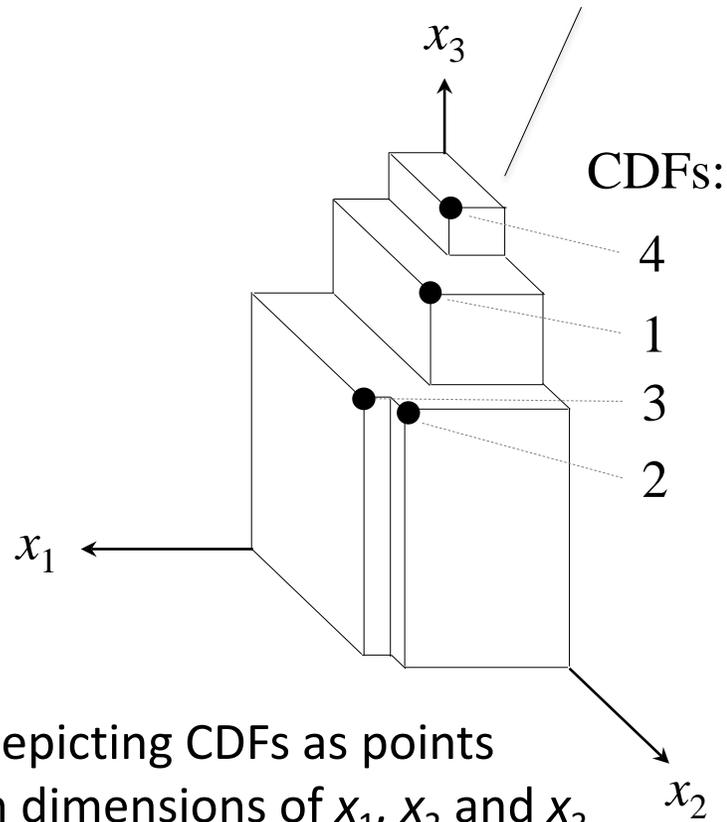
CDF 3: (0.45, 0.45, 0.55)

CDF 4: (0.125, 0.25, 1)



CDFs:   
 - Dashed line: 1   
 - Dotted line: 2   
 - Thick solid line: 3   
 - Thin solid line: 4

A hypervolume under a set of points 1-4 and a reference point  $r = (0,0,0)$



Depicting CDFs as points in dimensions of  $x_1, x_2$  and  $x_3$

Basic idea: calculate volumes of hyperspaces for points in non-dominant subsets...

...with these volumes, can arrange subsets in continuous space

# Comparing approaches via example

- ▶ Hypothetical invasive insect in North America
- ▶ Used CLIMEX to model its suitable range under current climate ... as well as ...

$$8 \times 3 \times 3 = 72$$

General  
Circulation  
Models

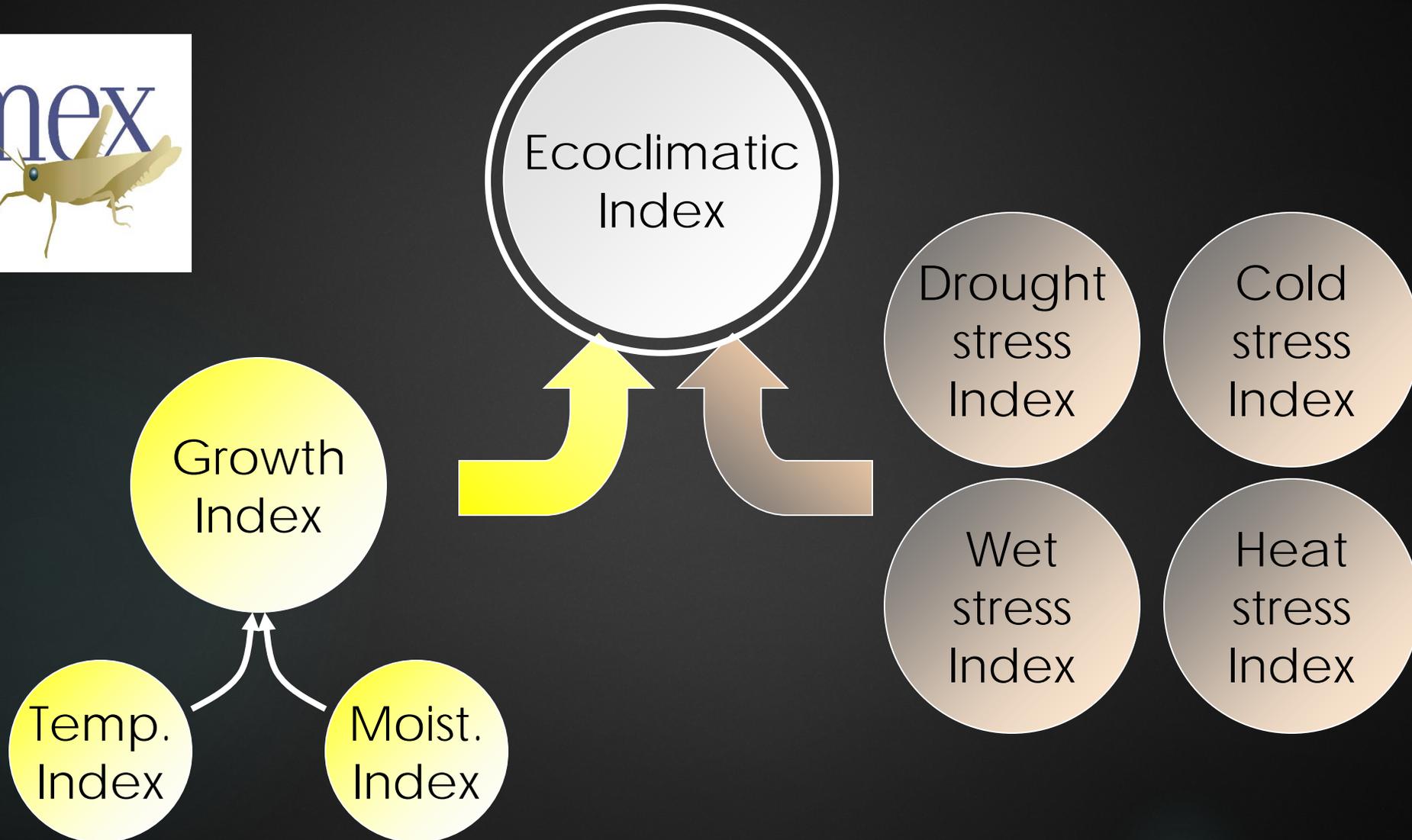
Emissions  
scenarios  
(a1, a2, b1)

Time horizons  
(2020, 2050,  
2080)

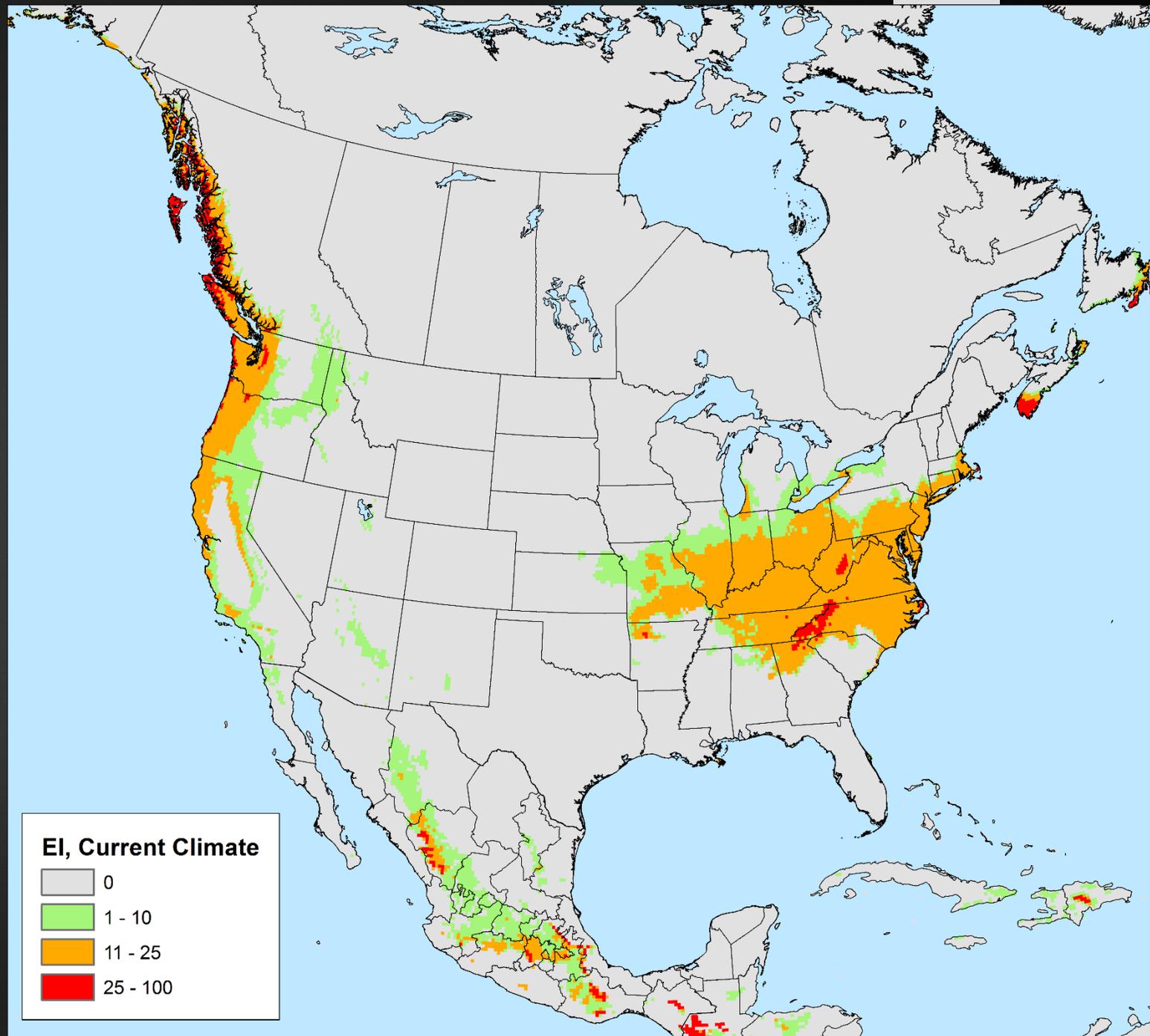
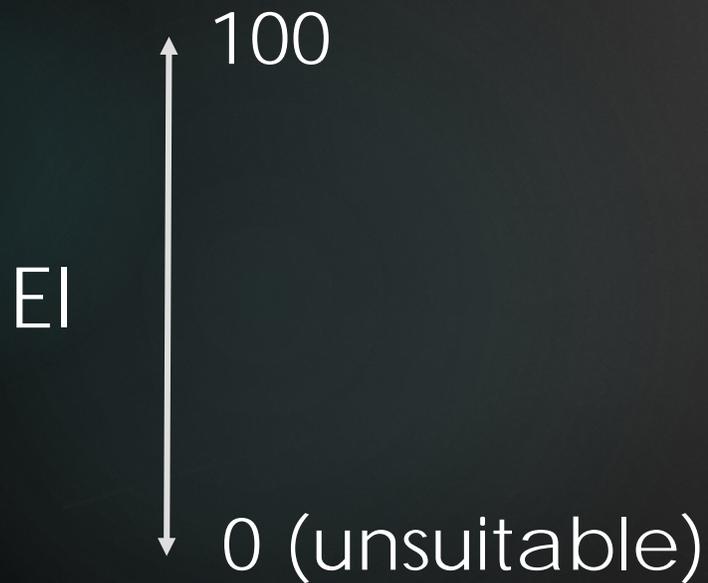
Projected  
outcomes

[Data provided by worldclim.org, downscaled to 30 arcsecond resolution]

# CLIMEX indices

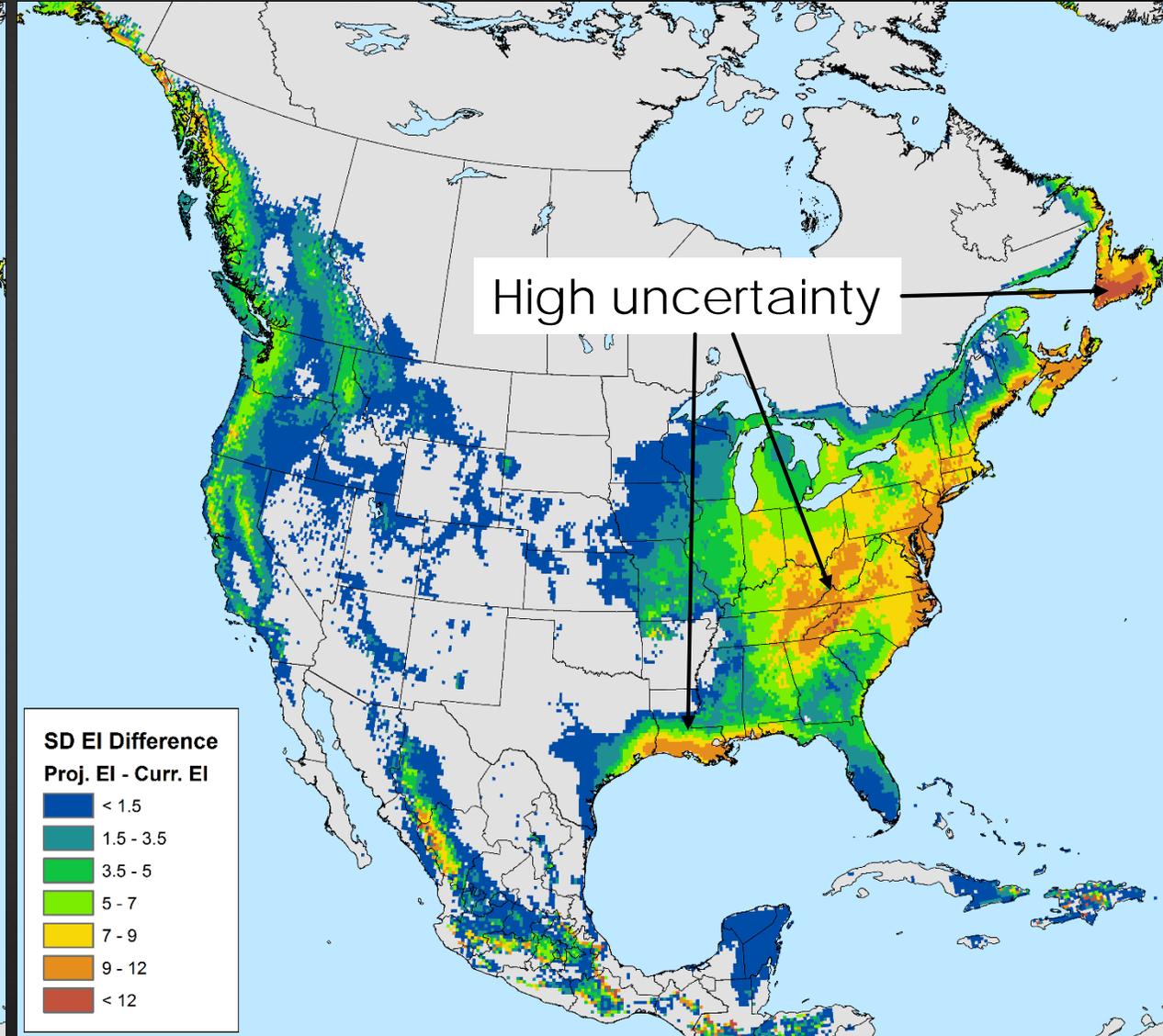
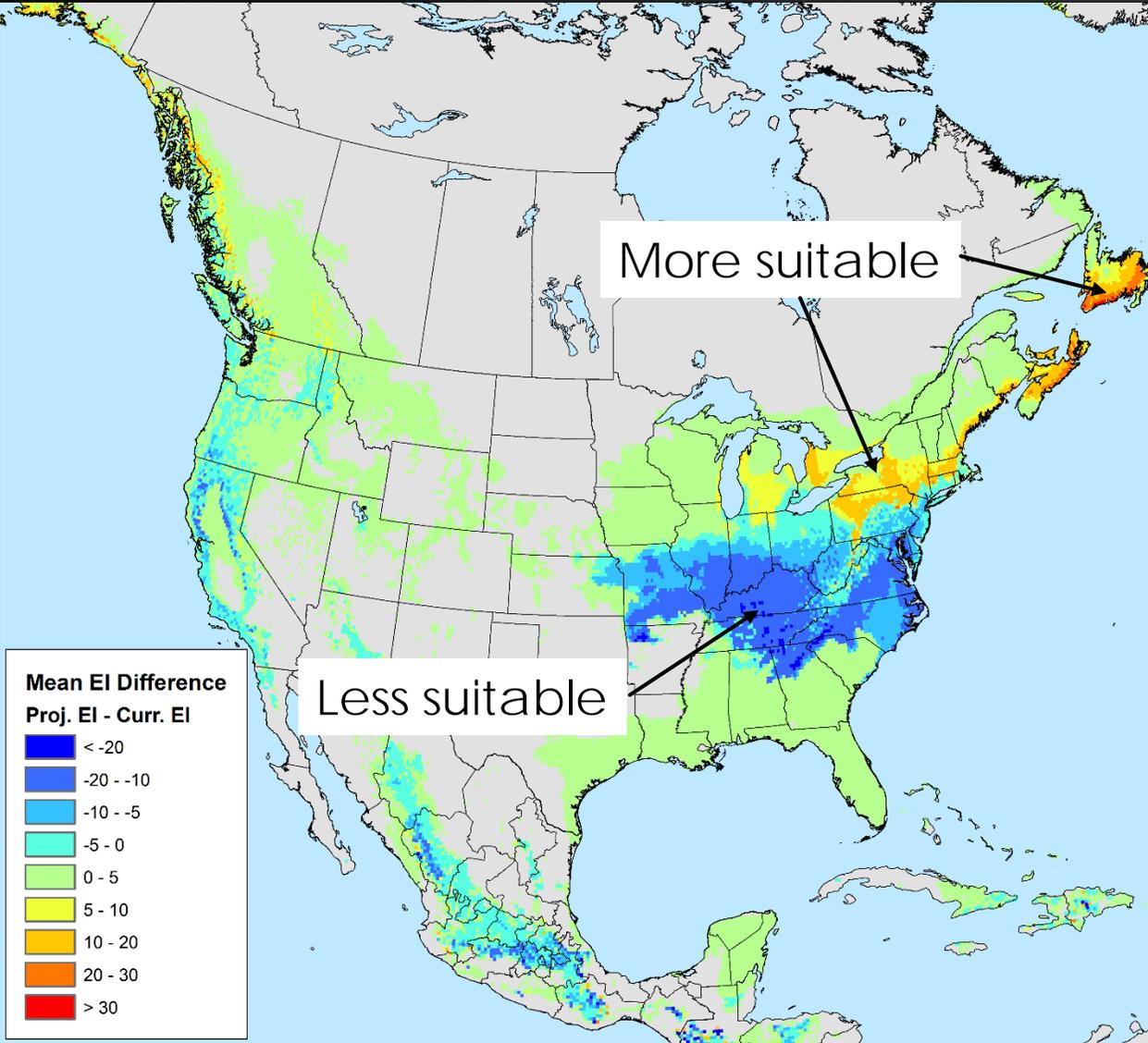


# Baseline EI under current climate



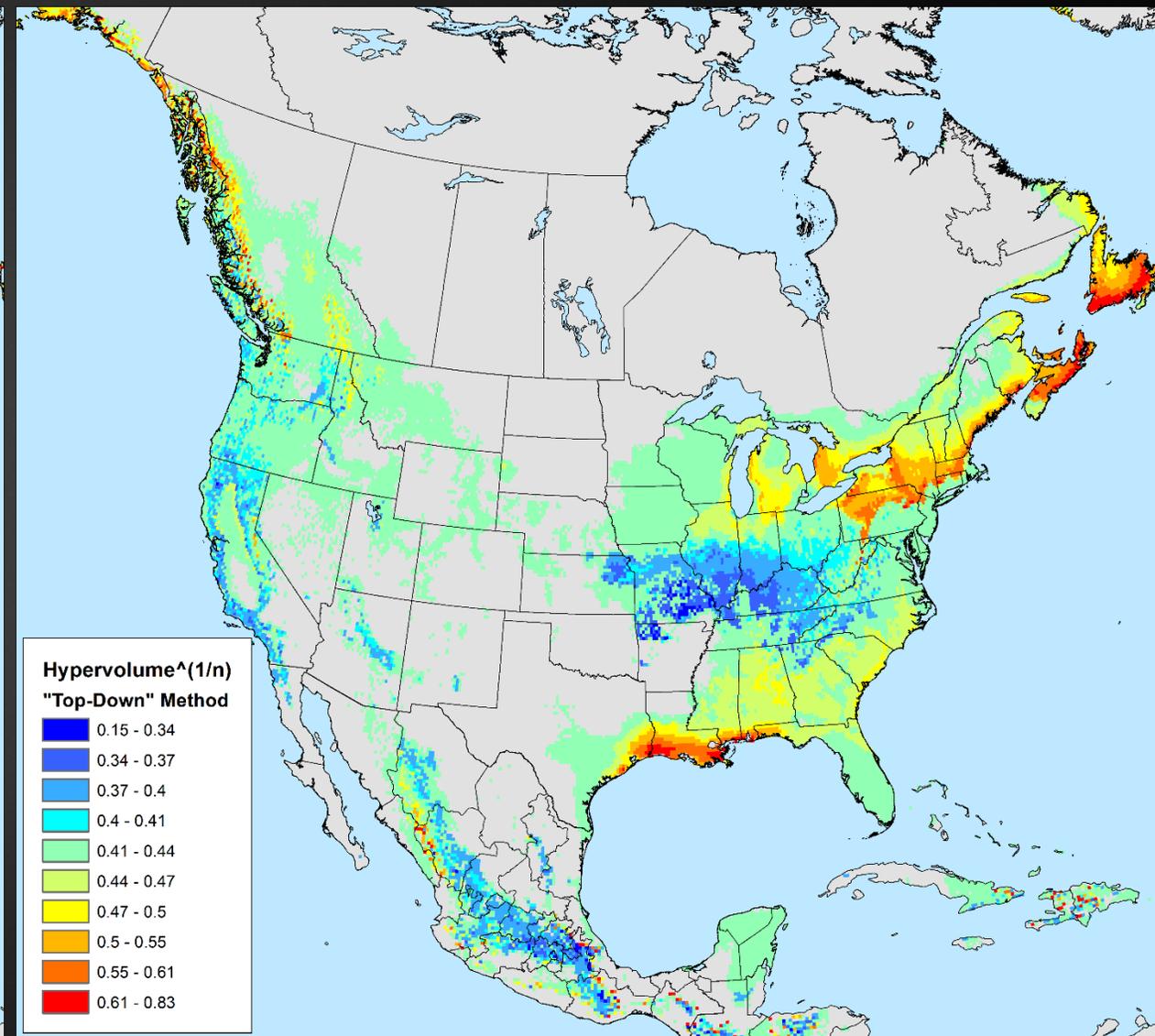
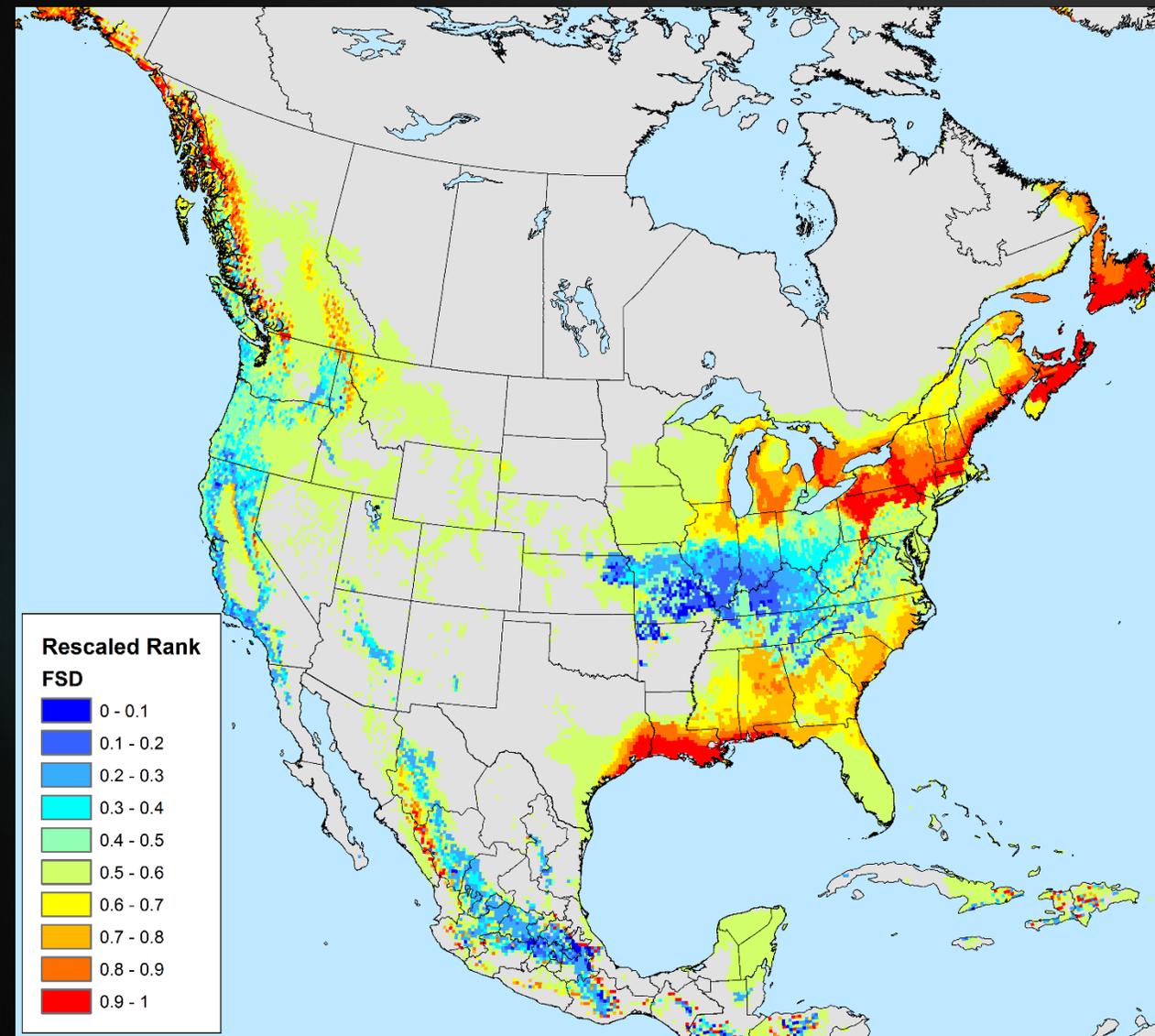
# Mean EI difference, projected – current climate

# Standard deviation of EI difference



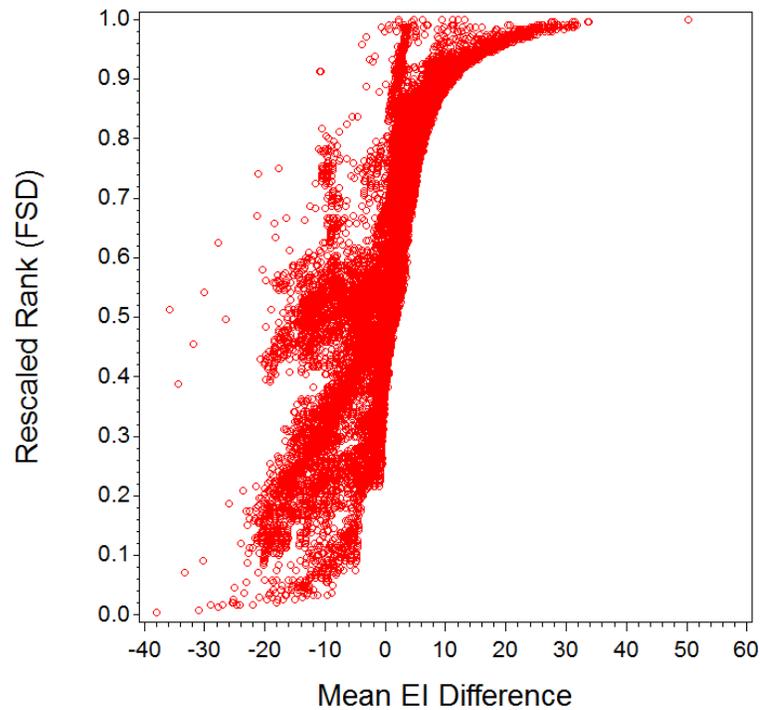
# Rescaled rank (0-1) from FSD

# Hypervolume<sup>(1/n)</sup>

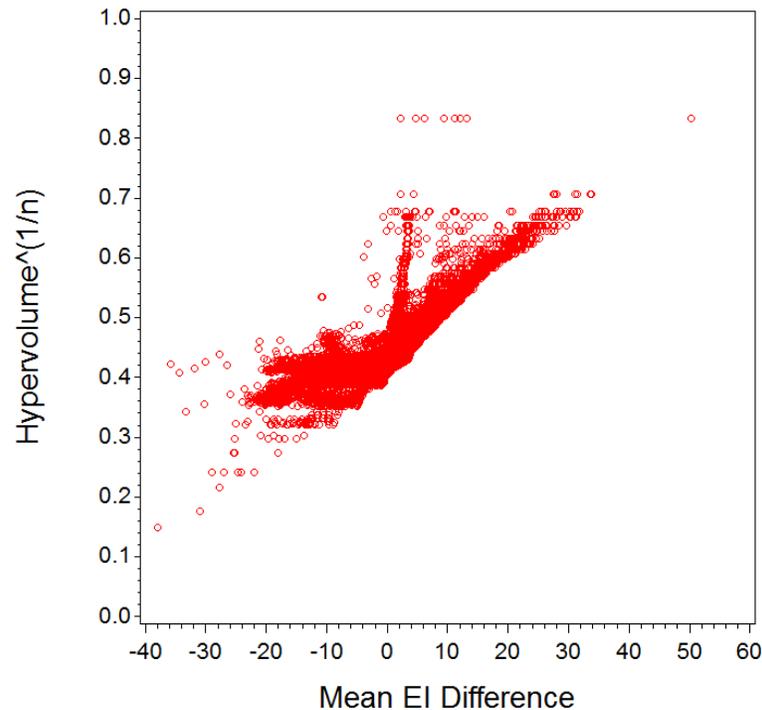


# Plotting measures against one another

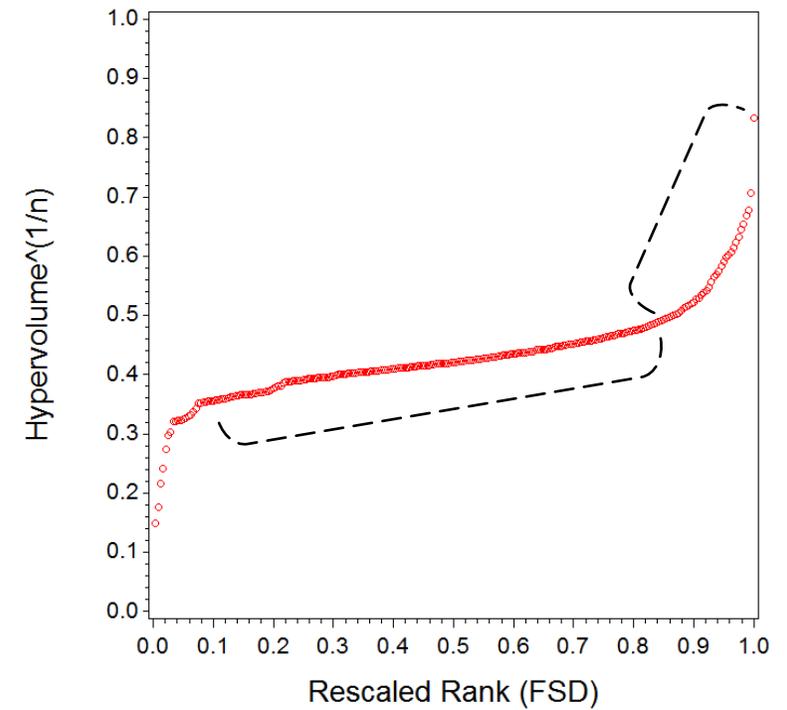
Rescaled rank (FSD)  
vs. mean EI difference



Hypervolume<sup>^(1/n)</sup>  
vs. mean EI difference



Hypervolume<sup>^(1/n)</sup>  
vs. rescaled rank (FSD)



# Summary points

- ▶ Both FSD and the hypervolume measure incorporate uncertainty
  - ▶ Only dealing with “known unknowns”
- ▶ Theoretically, hypervolume measure better than FSD alone
  - ▶ More information at top (and bottom) of scale
  - ▶ Is this important in practical terms?
- ▶ Can use hypervolume measure to compare species
  - ▶ Assuming consistent underlying metric, sampling intervals

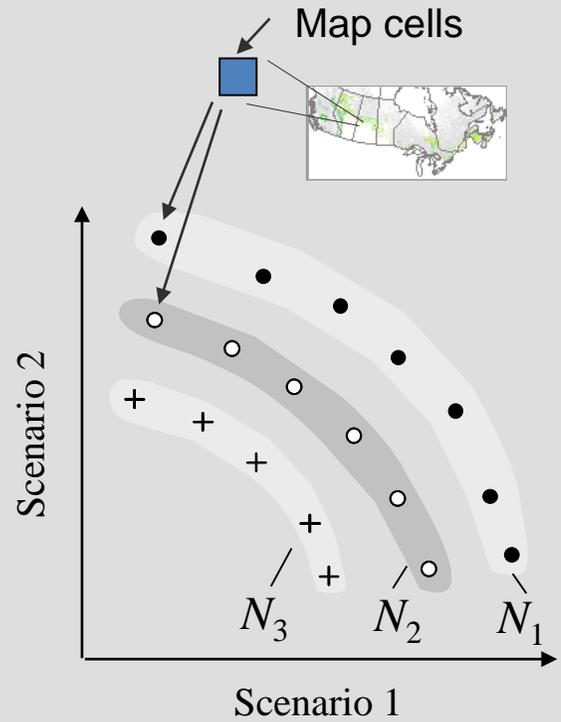


# Additional thoughts

- ▶ Outlined approach works well when only considering climate
  - ▶ Underlying criteria highly correlated
- ▶ But what about other, uncorrelated factors?
  - ▶ For example, economic and geopolitical factors
  - ▶ May have disparate (and highly uncertain) outcomes
- ▶ In this case, scenario analysis may be appropriate
  - ▶ Can still use hypervolumes
  - ▶ Instead of FSD, use multi-attribute frontier aggregation (MAFs)

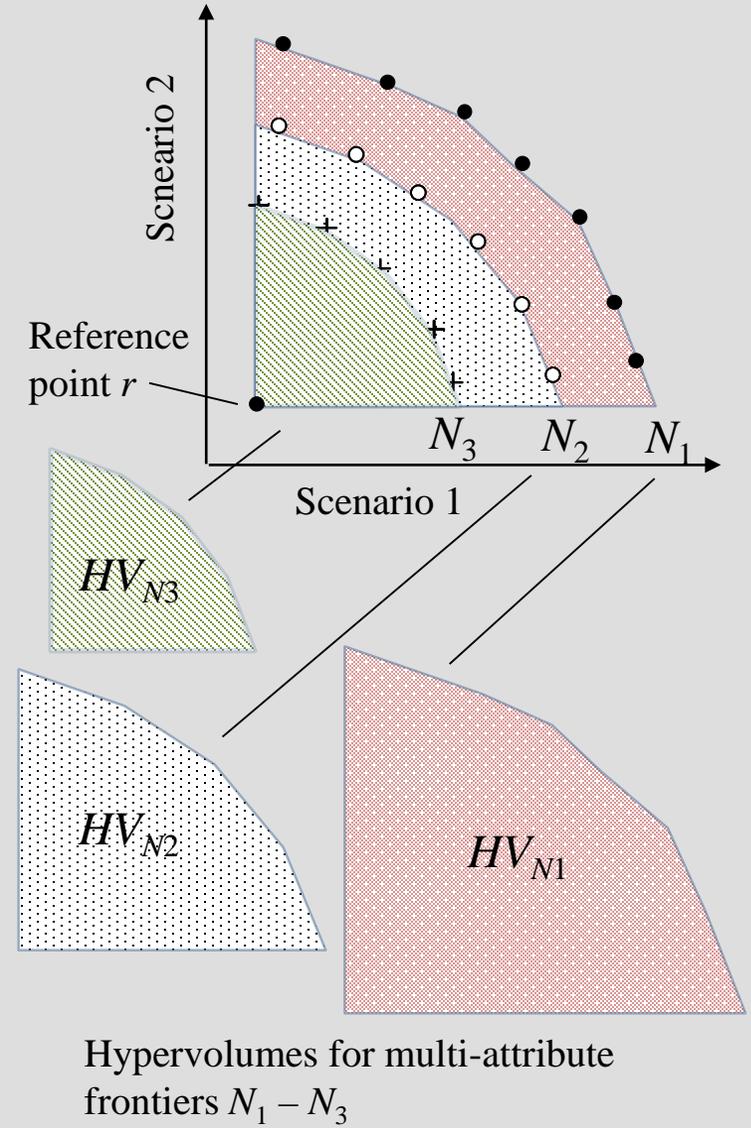
# Scenario analysis: 2D example

- ▶ Scenario 1 = Northwest Passage
  - ▶ Stronger connection between northern Europe and western North America
- ▶ Scenario 2 = Panama Canal
  - ▶ Stronger connection between eastern Asia and eastern North America
- ▶ Practical limit is about 10-15 scenarios



Multi-attribute frontiers:

- - Multi-attribute frontier  $N_1$  (dominates frontiers  $N_2$  and  $N_3$ )
- -  $N_2$  (dominates  $N_3$ , dominated by  $N_1$ )
- + -  $N_3$  (dominated by  $N_1$  and  $N_2$ )



Hypervolumes for multi-attribute frontiers  $N_1 - N_3$

# Questions?

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